

第8期
3~4版

一、选择题

1~5.CBCDB 6~10.BDCDA

二、填空题

11. $\frac{1}{2}$ 12.9.7

13. $\frac{5}{2}$ 14.(1)2;(2) $y=\frac{1}{x-1}$

三、

15.解:如图,△A₁B₁C和△A₂B₂C为所作图形.(画出一个即可)

(第15题图)

16.解:∵DE∥BC, ∴△ADE∽△ABC. ∴ $\frac{S_{\triangle ABC}}{S_{\triangle ADE}} = \left(\frac{BC}{DE}\right)^2 = \left(\frac{5}{2}\right)^2 = \frac{25}{4}$. 又∵S_{△ABC}=20, ∴S_{△ADE}= $\frac{16}{5}$.

四、

17.(1)证明:∵AB=2,BC=4,BD=1, $\frac{BD}{AB} = \frac{AB}{BC} = \frac{1}{2}$. ∴∠ABD=∠CBA, ∴△ABD∽△CBA. (2)解:由(1)知,△ABD∽△CBA. $\frac{BD}{AB} = \frac{AD}{AC}$. ∵AD=2.5,AB=2,BD=1, $\frac{2.5}{AC} = \frac{1}{2}$. ∴AC=5.

18.解:40 cm=0.4 m,20 cm=0.2 m. ∴∠D=∠D,∠DEF=∠DCB=90°, ∴△DEF∽△DCB. $\frac{DE}{CD} = \frac{EF}{BC}$,即 $\frac{0.4}{8} = \frac{0.2}{BC}$. 解得BC=4. ∴AC=1.5, ∴AB=AC+BC=1.5+4=5.5(m). 答:树高AB为5.5 m.

五、

19.解:(1)∵在Rt△ABC中,∠ACB=90°,AB=√6,AC=2, ∴BC=√(AB²-AC²)=√((√6)²-2²)=√2. 当△ABD∽△ACB时, $\frac{AB}{AC} = \frac{AD}{AB}$,即 $\frac{\sqrt{6}}{2} = \frac{AD}{\sqrt{6}}$. 解得AD=3. 当△ABD∽△BCA时, $\frac{AB}{BC} = \frac{AD}{AB}$,即 $\frac{\sqrt{6}}{\sqrt{2}} = \frac{AD}{\sqrt{6}}$. 解得AD=3√2. 综上,AD的长为3或3√2. (2)当△ABD∽△ACB时,

$\frac{S_{\triangle ABD}}{S_{\triangle ABC}} = \left(\frac{AD}{AB}\right)^2 = \left(\frac{3}{\sqrt{6}}\right)^2 = \frac{3}{2}$; 当△ABD∽△BCA时, $\frac{S_{\triangle ABD}}{S_{\triangle ABC}} = \left(\frac{AD}{AB}\right)^2 = \left(\frac{3\sqrt{2}}{\sqrt{6}}\right)^2 = 3$.

综上,△ABD与△ABC的面积比为 $\frac{3}{2}$ 或3.

20.解:(1)∵等边△A₁B₁C₁的边长为1,点O是B₁C₁的中点,点A₂是OA₁的中点, ∴等边△A₂B₂C₂的边长为 $\frac{1}{2}$. 由此类推,等边△A₁₀B₁₀C₁₀的边长为 $\left(\frac{1}{2}\right)^9$,等边△A₇B₇C₇的边长为 $\left(\frac{1}{2}\right)^6$. ∴等边△A₁₀B₁₀C₁₀和等边△A₇B₇C₇的相似比为 $\frac{\left(\frac{1}{2}\right)^9}{\left(\frac{1}{2}\right)^6} = \frac{1}{8}$,它们的位似中心为点O.

(2)∵第n个等边△A_nB_nC_n(n≥2)的边长为 $\left(\frac{1}{2}\right)^{n-1}$, ∴第n个等边△A_nB_nC_n(n≥2)的周长为 $\frac{3}{2^{n-1}}$.

六、

21.(1)证明:∵AB=AD, ∴∠ABD=∠ADB. ∵AD∥BC, ∴∠ADB=∠DBC. ∴∠DBC=∠ABD= $\frac{1}{2}$ ∠ABC=35°. ∴∠ADC+∠C=180°,∠ADC=145°, ∴∠C=35°. ∴∠ADB=∠ABD=∠DBC=∠C. ∴△ABD∽△DBC. ∴对角线BD是四边形ABCD的“理想对角线”. (2)解:∵对角线AC是四边形ABCD的“理想对角线”,CA平分∠BCD, ∴∠ACB=∠DCA. $\frac{DC}{AC} = \frac{AC}{BC}$. ∴AC²=DC·BC=3×2=6. 解得AC=√6(负值舍去). ∴AC的长为√6.

七、

22.(1)证明:∵立杆AB,CD相交于点O, ∴∠AOC=∠EOF. 又 $\frac{OA}{OE} = \frac{OC}{OF} = \frac{51}{34} = \frac{3}{2}$, ∴△AOC∽△EOF. ∴∠A=∠OEF. ∴AC∥EF. (2)解:如图,过点A作AM⊥BD于点M,过点O作ON⊥EF于点N.

(第22题图)

$\because OE=OF=34,$
 $\therefore \triangle OEF$ 是等腰三角形.
 $\therefore \angle OEF=\frac{1}{2}(180^\circ-\angle EOF).$
 $\therefore ON\perp EF, EF=32,$
 $\therefore ON$ 是边 EF 上的中线.
 $\therefore EN=16.$
在Rt△OEN中,根据勾股定理,得
 $ON=\sqrt{OE^2-EN^2}=\sqrt{34^2-16^2}=30.$
 $\therefore ON\perp EF, AM\perp BD,$
 $\therefore \angle ONE=\angle AMB=90^\circ.$
 $\therefore OA=OC, AB=CD,$
 $\therefore OB=OD.$
 $\therefore \angle OBD=\frac{1}{2}(180^\circ-\angle BOD).$
 $\therefore \angle OBD=\angle OEF.$
 $\therefore \triangle EON\sim\triangle BAM.$
 $\therefore \frac{OE}{AB}=\frac{ON}{AM},$ 即 $\frac{34}{136}=\frac{30}{AM}.$
解得 $AM=120(\text{cm}).$
答:利用夹子垂挂在晾衣架上的连衣裙总长度小于120 cm时,连衣裙才不会拖在地面上.

八、

23.解:(1) $AD\perp BE$ (或垂直). (2)(1)中的结论成立. 证明:延长BE交AD于点N. $\therefore \angle ACB=\angle DCE=90^\circ,$
 $\therefore \angle ACD=\angle BCE.$
又 $\therefore \frac{DC}{CE}=\frac{AC}{BC}=\frac{1}{m},$
 $\therefore \triangle DCA\sim\triangle ECB.$
 $\therefore \angle DAC=\angle CBE.$
 $\therefore \angle CAB+\angle ABE+\angle CBE=90^\circ,$
 $\therefore \angle CAB+\angle ABE+\angle DAC=90^\circ.$
 $\therefore \angle ANB=90^\circ.$
 $\therefore AD\perp BE.$ (3)如图①,当点E在线段AD上时,连接BE.

(第23题图)

如图②,当点D在线段AE上时,连接BE. $\therefore \triangle DCA\sim\triangle ECB,$
 $\frac{BE}{AD}=\frac{BC}{AC}=m=\sqrt{3}.$
 $\therefore BE=\sqrt{3}AD=\sqrt{3}(4+AE).$
 $\therefore AD\perp BE,$
 $\therefore AB^2=AE^2+BE^2,$
即 $(4\sqrt{7})^2=AE^2+3(4+AE)^2.$
解得AE=2(负值舍去).
 $\therefore BE=6\sqrt{3}.$
综上,BE的长为 $6\sqrt{3}$ 或 $4\sqrt{3}.$

数学
沪科

中考版答案页第2期

第5期

2版

22.1比例线段

第1课时

1.D

2.(1)×;(2)×;(3)√;(4)√;(5)√;(6)×

3.解:(1)∵四边形ABCD与四边形EFGH是相似图形,且点A与点E,点B与点F,点C与点G,点D与点N分别是对应顶点, ∴四边形ABCD与四边形EFGH的相似比为 $\frac{AD}{EH}=\frac{1.8}{1.2}=\frac{3}{2}.$ (2)∵四边形ABCD与四边形EFGH是相似图形, $\therefore BC:FG=AB:EF=AD:EH=3:2.$
 $\therefore FG=2.8, AB=3.6,$
 $\therefore BC=4.2, EF=2.4.$

第2课时

1.A

2.6

3.解:(1)∵AB=8 cm,BC=12 cm,A'B'=4 cm,B'C'=6 cm, $\frac{A'B'}{AB}=\frac{4}{8}=\frac{1}{2}, \frac{B'C'}{BC}=\frac{6}{12}=\frac{1}{2}.$ (2)由(1)知, $\frac{A'B'}{AB}=\frac{1}{2}, \frac{B'C'}{BC}=\frac{1}{2},$
 $\therefore \frac{A'B'}{AB}=\frac{B'C'}{BC}.$
∴线段A'B',AB,B'C',BC是成比例线段.

第3课时

1.B

2.A

3. $\frac{5}{2}$

4.170

5. $5\sqrt{5}-5$

6.解:△ABC是等边三角形. 理由:∵a,b,c是△ABC三边的长, $\therefore a+b+c\neq 0.$
 $\therefore \frac{a-b}{b}=\frac{b-c}{c}=\frac{c-a}{a},$
 $\therefore \frac{a-b}{b}=\frac{b-c}{c}=\frac{c-a}{a}=\frac{a-b+b-c+c-a}{b+c+a}=0.$
 $\therefore a-b=0, b-c=0, c-a=0.$
 $\therefore a=b=c.$

∴△ABC是等边三角形.

第4课时

1.C 2.C

3.解:∵DE∥BC, $\frac{AD}{DB}=\frac{2}{3},$
 $\therefore \frac{AE}{EC}=\frac{AD}{DB}=\frac{2}{3}.$
∴EF∥AB, $\therefore \frac{BF}{CF}=\frac{AE}{EC}=\frac{2}{3},$
即 $\frac{BF}{BC-BF}=\frac{2}{3}.$
∴BC=20,
∴BF=8.

3版

一、选择题

1~5.CADDA 6~10.CCCBC

二、填空题

11.2:3

12.16

13. $\frac{3}{7}$

14. $\frac{5-2\sqrt{5}}{2}$

三、解答题

15.解:∵CD⊥BC,∴∠C=90°. ∴四边形A'B'C'D'与四边形ABCD相似, $\therefore \angle B'=\angle B=65^\circ, \angle C'=\angle C=90^\circ,$
 $\frac{A'B'}{AB}=\frac{B'C'}{BC}=\frac{A'D'}{AD}.$
 $\therefore \frac{x}{21}=\frac{12}{y}=\frac{10}{15}.$
 $\therefore x=14, y=18.$
 $\therefore \alpha=\angle D'=360^\circ-\angle A'-\angle B'-\angle C'=360^\circ-135^\circ-65^\circ-90^\circ=70^\circ.$

16.解:∵ $\frac{2a}{b+c+d}=\frac{2b}{a+c+d}=\frac{2c}{a+b+d}=\frac{2d}{a+b+c}=k,$
 $\therefore \frac{2(a+b+c+d)}{3(a+b+c+d)}=k.$
当a+b+c+d≠0时,可得 $k=\frac{2}{3}.$
当a+b+c+d=0时, $b+c+d=-a,$
 $\therefore k=\frac{2a}{b+c+d}=\frac{2a}{-a}=-2.$

当 $k=\frac{2}{3}$ 时, $k^2-3k-4=\left(\frac{2}{3}\right)^2-3\times\frac{2}{3}-4=-\frac{50}{9};$
当 $k=-2$ 时, $k^2-3k-4=(-2)^2-3\times(-2)-4=6.$
综上, k^2-3k-4 的值为 $-\frac{50}{9}$ 或6.

17.解:(1)不相似. 理由:∵AB=20 m,AD=30 m,小路的宽度为2 m, $\therefore EF=AB+2\times 2=24(\text{m}), EH=AD+2\times 2=34(\text{m}).$
 $\therefore \frac{AB}{EF}=\frac{20}{24}=\frac{5}{6}, \frac{AD}{EH}=\frac{30}{34}=\frac{15}{17},$
 $\therefore \frac{AB}{EF}\neq\frac{AD}{EH}.$
∴矩形ABCD与矩形EFGH不相似. (2)∵相对两条小路的宽度相等, $\therefore EF=AB+2y=(20+2y)\text{ m}, EH=AD+2x=(30+2x)\text{ m}.$
∴矩形EFGH与矩形ABCD相似, $\therefore \frac{EF}{AB}=\frac{EH}{AD},$ 即 $\frac{20+2y}{20}=\frac{30+2x}{30}.$
 $\therefore \frac{x}{y}=\frac{3}{2}.$
∴小路的宽度x与y的比值为 $\frac{3}{2}.$

18.解:(1)证明:如图②,过点C作CE∥DA,交BA的延长线于点E. $\therefore \frac{AB}{AE}=\frac{BD}{CD}, \angle CAD=\angle ACE, \angle BAD=\angle E.$
∴AD平分∠BAC, $\therefore \angle BAD=\angle CAD.$
∴∠ACE=∠E. $\therefore AE=AC.$
 $\therefore \frac{AB}{AC}=\frac{BD}{CD}.$ (2)∵AD是角平分线, $\therefore \frac{AB}{AC}=\frac{BD}{CD}.$
∴AB=5 cm,AC=4 cm,BC=7 cm, $\therefore \frac{5}{4}=\frac{BD}{7-BD}.$
解得BD= $\frac{35}{9}.$
∴BD的长为 $\frac{35}{9}$ cm. (3)10.

第4页

第1页

1.A 2.D

3.解: ∵ $\frac{AE}{AB} = \frac{2}{3}$, ∴ $\frac{AE}{BE} = \frac{2}{5}$.

∵ $AG \parallel BC$,

∴ $\triangle EAG \sim \triangle EBD$.

∴ $\frac{AG}{BD} = \frac{AE}{BE} = \frac{2}{5}$.

∵ 点D是边BC的中点, ∴ $DC = BD$.

∴ $\frac{AG}{DC} = \frac{2}{5}$.

∵ $AG \parallel BC$, ∴ $\triangle AGF \sim \triangle CDF$.

∴ $\frac{AF}{FC} = \frac{AG}{DC} = \frac{2}{5}$.

1.D 2.B

3.证明: ∵ 四边形ABCD为矩形,

∴ $\angle BAD = \angle D = 90^\circ$.

∴ $\angle DAE + \angle BAE = 90^\circ$.

∵ $BF \perp AE$ 于点F, ∴ $\angle BFA = 90^\circ$.

∴ $\angle ABF + \angle BAE = 90^\circ$.

∴ $\angle ABF = \angle DAE$.

又 ∵ $\angle BFA = \angle D = 90^\circ$,

∴ $\triangle ABF \sim \triangle EAD$.

1.B

2. 54 或 $\frac{75}{2}$

3.解: (1) 答案不唯一, 如添加的条件是 $\angle ADC = \angle ABC$.

证明: ∵ $\angle BAD = \angle CAE$,

∴ $\angle BAD + \angle BAE = \angle BAE + \angle CAE$, 即

$\angle DAE = \angle BAC$.

又 ∵ $\angle ADC = \angle ABC$,

∴ $\triangle ADE \sim \triangle ABC$.

(2) $\triangle ABD \sim \triangle ACE$.

理由: ∵ $\triangle ADE \sim \triangle ABC$,

∴ $\frac{AB}{AD} = \frac{AC}{AE}$.

∴ $\frac{AB}{AC} = \frac{AD}{AE}$.

又 ∵ $\angle BAD = \angle CAE$,

∴ $\triangle ABD \sim \triangle ACE$.

1.相似

2.解: $\triangle ABC$ 与 $\triangle DEF$ 相似.

理由: 根据题意, 得 $AB = 2, DE = 1$.

由勾股定理, 可得 $AC = 2\sqrt{5}, BC =$

$4\sqrt{2}, DF = \sqrt{5}, EF = 2\sqrt{2}$.

∴ $\frac{AB}{DE} = 2, \frac{AC}{DF} = \frac{2\sqrt{5}}{\sqrt{5}} = 2, \frac{BC}{EF} = \frac{4\sqrt{2}}{2\sqrt{2}} =$

2,

∴ $\frac{AB}{DE} = \frac{AC}{DF} = \frac{BC}{EF}$.

∴ $\triangle ABC \sim \triangle DEF$.

1.D

2.证明: ∵ $BF = 3, CF = 5$,

∴ $BC = BF + CF = 8$.

∵ $\angle B = 90^\circ, AB = 6$,

由勾股定理, 可得 $AC = 10$.

∴ $\frac{AB}{DE} = \frac{6}{15} = \frac{2}{5}, \frac{AC}{DF} = \frac{10}{25} = \frac{2}{5}$,

∴ $\frac{AB}{DE} = \frac{AC}{DF}$.

又 ∵ $\angle B = \angle E = 90^\circ$,

∴ $\triangle ABC \sim \triangle DEF$.

一、选择题

1~5.DAABD 6~10.ACCBA

二、填空题

11. 答案不唯一, 如 $\angle ADE = \angle B$

12. $\triangle ADC$ 和 $\triangle ACB$

13. 5

14. $\frac{25}{8}$ 或 $\frac{20}{7}$

三、解答题

15. 证明: ∵ $AD = 1, AB = 3, AC = \sqrt{3}$,

∴ $\frac{AC}{AB} = \frac{\sqrt{3}}{3}, \frac{AD}{AC} = \frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{3}$.

∴ $\frac{AD}{AC} = \frac{AC}{AB}$.

又 ∵ $\angle A = \angle A$,

∴ $\triangle ACD \sim \triangle ABC$.

16. (1) 证明: ∵ $CA \perp AD, CB \perp BE$,

$ED \perp AD$,

∴ $\angle A = \angle CBE = \angle D = 90^\circ$.

∴ $\angle C + \angle CBA = 90^\circ, \angle CBA + \angle DBE =$

90° .

∴ $\angle C = \angle DBE$.

∴ $\triangle ABC \sim \triangle DEB$.

(2) 解: ∵ $\triangle ABC \sim \triangle DEB$,

∴ $\frac{AC}{BD} = \frac{AB}{DE}$, 即 $\frac{6}{BD} = \frac{8}{4}$.

解得 $BD = 3$.

∴ 线段BD的长为3.

17. (1) 证明: ∵ 四边形ABCD为正方形,

∴ $AD = AB = DC = BC, \angle A = \angle D = 90^\circ$.

∵ $AE = ED$, ∴ $\frac{AE}{AB} = \frac{1}{2}$.

∵ $DF = \frac{1}{4}DC$, ∴ $\frac{DF}{ED} = \frac{1}{2}$.

∴ $\frac{AE}{AB} = \frac{DF}{ED}$, 即 $\frac{AE}{DF} = \frac{AB}{ED}$.

∴ $\triangle ABE \sim \triangle DEF$.

(2) 解: ∵ 四边形ABCD为正方形,

∴ $ED \parallel BG$.

∴ $\triangle EDF \sim \triangle GCF$.

∴ $\frac{ED}{CG} = \frac{DF}{CF}$.

∴ $DF = \frac{1}{4}DC, AE = ED$, 正方形ABCD

的边长为4,

∴ $DF = 1, CF = 3, ED = 2$.

∴ $CG = 6$.

∴ $BG = BC + CG = 4 + 6 = 10$.

18. 解: (1) 当 $PQ \parallel BC$ 时, $AP : AB =$

$AQ : AC$.

∴ $AP = 4x, AQ = 30 - 3x$,

∴ $\frac{4x}{20} = \frac{30 - 3x}{30}$.

解得 $x = \frac{10}{3}$.

∴ 当 $x = \frac{10}{3}$ 时, $PQ \parallel BC$.

(2) $\triangle APQ$ 与 $\triangle CQB$ 能相似.

∵ $BA = BC$, ∴ $\angle A = \angle C$.

① 当 $\frac{AP}{CQ} = \frac{AQ}{BC}$ 时, $\triangle APQ \sim \triangle CQB$.

∴ $\frac{4x}{3x} = \frac{30 - 3x}{20}$.

解得 $x = \frac{10}{9}$.

∴ $AP = 4x = \frac{40}{9}$ (cm).

② 当 $\frac{AP}{BC} = \frac{AQ}{CQ}$ 时, $\triangle APQ \sim \triangle CBQ$.

∴ $\frac{4x}{20} = \frac{30 - 3x}{3x}$.

解得 $x_1 = 5, x_2 = -10$ (舍去).

∴ $AP = 4x = 20$ (cm).

综上, 当AP的长为 $\frac{40}{9}$ cm 或 20 cm

时, $\triangle APQ$ 与 $\triangle CQB$ 相似.

1.D 2.C 3.k

4. 证明: ∵ $\frac{AB}{A_1B_1} = \frac{AD}{A_1D_1} = \frac{BD}{B_1D_1}$,

∴ $\text{Rt} \triangle ABD \sim \text{Rt} \triangle A_1B_1D_1$.

∴ $\angle ABC = \angle A_1B_1C_1$.

又 ∵ $\angle C = \angle C_1$,

∴ $\triangle ABC \sim \triangle A_1B_1C_1$.

又 ∵ $\frac{AD}{A_1D_1} = \frac{AB}{A_1B_1}$,

∴ $\frac{AD}{A_1D_1} = \frac{BE}{B_1E_1}$.

5.C 6.4.2

7. (1) 证明: ∵ $AB = 27, AC = 18, CD = 12$,

∴ $\frac{AB}{AC} = \frac{27}{18} = \frac{3}{2}, \frac{AC}{CD} = \frac{18}{12} = \frac{3}{2}$.

∴ $\frac{AB}{AC} = \frac{AC}{CD}$.

∴ $AB \parallel CD$,

∴ $\angle BAC = \angle ACD$.

∴ $\triangle ABC \sim \triangle CAD$.

(2) 解: 由(1)可知, $\triangle ABC \sim \triangle CAD$.

∴ $\frac{S_{\triangle ABC}}{S_{\triangle CAD}} = \left(\frac{AB}{AC}\right)^2 = \left(\frac{3}{2}\right)^2 = \frac{9}{4}$.

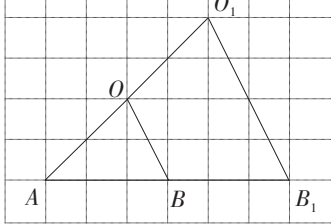
∴ $\triangle ACD$ 的面积为 80 m^2 ,

∴ $\triangle ABC$ 的面积为 $80 \times \frac{9}{4} = 180 (\text{m}^2)$.

答: 水果园 $\triangle ABC$ 的面积为 180 m^2 .

1.B 2.D 3.A 4.50

5. 解: 如图所示, $\triangle O_1AB_1$ 即为所求.



(第5题图)

22.5综合与实践 测量与误差

解: ∵ $AD \parallel EG$,

∴ $\angle ADO = \angle EGF$.

又 ∵ $\angle AOD = \angle EFG = 90^\circ$,

∴ $\triangle AOD \sim \triangle EFG$.

∴ $\frac{AO}{EF} = \frac{OD}{FG}$, 即 $\frac{AO}{1.8} = \frac{20}{2.4}$.

解得 $AO = 15$.

同理, 得 $\triangle BOC \sim \triangle AOD$.

∴ $\frac{BO}{AO} = \frac{OC}{OD}$, 即 $\frac{BO}{15} = \frac{16}{20}$.

解得 $BO = 12$.

∴ $AB = AO - BO = 15 - 12 = 3$ (m).

答: 旗杆AB的高是3 m.

一、选择题

1~5.DADCD

6~10.DDCBC

二、填空题

11.4.5

12.(2,1)

13.48

14.21.2

三、解答题

15. 解: (1) ∵ $\triangle ABC \sim \triangle A'B'C'$,

$\frac{AB}{A'B'} = \frac{1}{2}$,

∴ $\frac{CD}{C'D'} = \frac{1}{2}$.

∴ $CD = 4 \text{ cm}$,

∴ $C'D' = 4 \times 2 = 8$ (cm).

(2) ∵ $\triangle ABC \sim \triangle A'B'C'$, $\frac{AB}{A'B'} = \frac{1}{2}$,

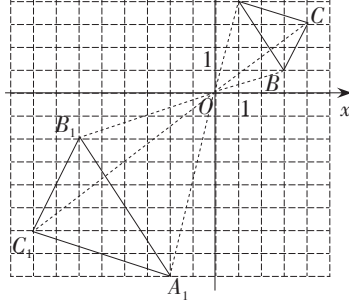
∴ $\frac{C_{\triangle ABC}}{C_{\triangle A'B'C'}} = \frac{1}{2}$.

∴ $\triangle ABC$ 的周长为 20 cm ,

∴ $C_{\triangle A'B'C'} = 20 \times 2 = 40$ (cm).

∴ $\triangle A'B'C'$ 的周长为 40 cm .

16. 解: (1) 如图, $\triangle A_1B_1C_1$ 即为所求.



(第16题图)

(2) 14.

17. 解: 由题意可知, $AB \perp FN, MN \perp$

$FN, CD \perp FN$.

∴ $\angle N = \angle BAE = \angle DCF = 90^\circ$.

∴ $\angle BEA = \angle MEN$,

∴ $\triangle BEA \sim \triangle MEN$.

∴ $\frac{AB}{MN} = \frac{EA}{EN}$, 即 $\frac{1.5}{MN} = \frac{2}{2 + AN}$.①

同理可证, $\triangle FDC \sim \triangle FMN$,

∴ $\frac{DC}{MN} = \frac{FC}{FN}$, 即 $\frac{1.5}{MN} = \frac{4}{4 + 50 + AN}$.②

联立①②, 解得 $AN = 50, MN = 39$.

答: 古塔的高度为 39 m .

18. 解: (1) ∵ 四边形EGHF为正方形,

∴ $EF \parallel GH, EF = EG, \angle FEG = \angle EGH =$

90° .

∴ $\triangle AEF \sim \triangle ABC$.

∴ $\frac{EF}{BC} = \frac{AK}{AD}$.

∴ $AD \perp BC$,

∴ $\angle FEG = \angle EGD = \angle GDK = 90^\circ$.

∴ 四边形EGDK为矩形.

∴ $KD = EG = EF$.

∴ $\frac{EF}{120} = \frac{80 - EF}{80}$.

解得 $EF = 48$.

答: 这个正方形零件的边长为 48 mm .

(2) ∵ 四边形EGHF为矩形,

∴ $EF \parallel GH$, 即 $EF \parallel BC$.

∴ $\triangle AEF \sim \triangle ABC$.

∴ $\frac{EF}{BC} = \frac{AK}{AD} = \frac{AD - KD}{AD}$.

易证四边形EGDK为矩形,

∴ $KD = EG$.

设 $EG = x, EF = y$,

∴ $\frac{y}{120} = \frac{80 - x}{80}$.

∴ $y = -\frac{3}{2}x + 120$.

∴ $S = xy = x \left(-\frac{3}{2}x + 120 \right) = -\frac{3}{2}x^2 + 120x =$

$-\frac{3}{2}(x - 40)^2 + 2400$.

∴ $-\frac{3}{2} < 0$,

∴ 当 $x = 40 \text{ mm}$ 时, S最大, 最大值

为 2400 mm^2 .

答: 矩形EGHF的面积S的最大值

是 2400 mm^2 .